

**GIỚI HẠN DÃY SỐ**

- 1)  $\lim_{n \rightarrow \infty} \frac{6n^3 - 2n + 1}{n^3 - 2n}$
- 2)  $\lim_{n \rightarrow \infty} \frac{1 - n + 2n^2}{5n^2 + n}$
- 3)  $\lim_{n \rightarrow \infty} \frac{2n^3 - 4n^2 + 3n + 3}{n^3 - 5n + 7}$
- 4)  $\lim_{n \rightarrow \infty} \frac{-2n^2 + n + 2}{3n^4 + 5}$
- 5)  $\lim_{n \rightarrow \infty} \frac{n^2 + 4n - 5}{3n^3 + n^2 + 7}$
- 6)  $\lim_{n \rightarrow \infty} \frac{n^5 + n^4 - n - 2}{4n^3 + 6n^2 + 9}$
- 7)  $\lim_{n \rightarrow \infty} \frac{7n^2 - 3n + 2}{n^2 + 5}$
- 8)  $\lim_{n \rightarrow \infty} \frac{3n^3 + 2n - 1}{2n^2 - n}$
- 9)  $\lim_{n \rightarrow \infty} \left( \frac{2n^3}{2n^2 + 3} + \frac{1 - 5n^2}{5n + 1} \right)$
- 10)  $\lim_{n \rightarrow \infty} \frac{-3n^5 + 7n^3 - 11}{n^5 + n^4 - 3n}$
- 11)  $\lim_{n \rightarrow \infty} \frac{2n^2 - 3}{n^6 + 5n^5}$
- 12)  $\lim_{n \rightarrow \infty} \frac{\sqrt{2n^2 - n}}{1 - 3n^2}$
- 13)  $\lim_{n \rightarrow \infty} \frac{\sqrt[3]{n^3 + n}}{n + 2}$
- 14)  $\lim_{n \rightarrow \infty} \frac{\sqrt{2n^4 + 3n - 2}}{2n^2 - n + 3}$
- 15)  $\lim_{n \rightarrow \infty} \frac{\sqrt[3]{n^6 - 7n^3 - 5n + 8}}{n + 12}$
- 16)  $\lim_{n \rightarrow \infty} \frac{\sqrt{n^2 + 1} - \sqrt{n + 1}}{3n + 2}$
- 17)  $\lim_{n \rightarrow \infty} (3n^3 - 7n + 11)$
- 18)  $\lim_{n \rightarrow \infty} \sqrt{2n^4 - n^2 + n + 2}$
- 19)  $\lim_{n \rightarrow \infty} \sqrt[3]{1 + 2n - n^3}$
- 20)  $\lim_{n \rightarrow \infty} \frac{1 + 2 + \dots + n}{n^2}$
- 21)  $\lim_{n \rightarrow \infty} \frac{n\sqrt{2 + 4 + \dots + 2n}}{3n^2 + n - 2}$
- 22)  $\lim_{n \rightarrow \infty} \frac{1^3 + 2^3 + \dots + n^3}{n^4 + n^3 + 3n + 2}$
- 23)  $\lim_{n \rightarrow \infty} \frac{n\sqrt{1 + 3 + \dots + (2n-1)}}{2n^2 + n + 1}$
- 24)  $\lim_{n \rightarrow \infty} \frac{\sqrt{1^3 + 2^3 + \dots + n^3}}{11n^2 + n + 2}, 1^3 + 2^3 + \dots + n^3 = \frac{n^2(n+1)^2}{4}$
- 25)  $\lim_{n \rightarrow \infty} \frac{1 + \frac{2}{3} + \left(\frac{2}{3}\right)^2 + \dots + \left(\frac{2}{3}\right)^n}{1 + \frac{1}{5} + \left(\frac{1}{5}\right)^2 + \dots + \left(\frac{1}{5}\right)^n}$
- 26)  $\lim_{n \rightarrow \infty} \frac{4^n}{2 \cdot 3^n + 4^n}$
- 27)  $\lim_{n \rightarrow \infty} \frac{3^n + 1}{2^n - 1}$
- 28)  $\lim_{n \rightarrow \infty} \frac{3^n - 2.5^n}{7 + 3.5^n}$
- 29)  $\lim_{n \rightarrow \infty} \frac{4^n - 5^n}{2^n + 3.5^n}$
- 30)  $\lim_{n \rightarrow \infty} \frac{(-3)^n + 5^n}{(-3)^{n+1} + 5^{n+1}}$
- 31)  $\lim_{n \rightarrow \infty} (\sqrt{3n-1} - \sqrt{2n-1})$
- 32)  $\lim_{n \rightarrow \infty} (\sqrt{n+1} - \sqrt{n})\sqrt{n}$
- 33)  $\lim_{n \rightarrow \infty} (\sqrt{n^2 + n + 1} - n)$
- 37)  $\lim_{n \rightarrow \infty} n^2 (n - \sqrt{n^2 + 1})$
- 34)  $\lim_{n \rightarrow \infty} (\sqrt{n^2 + n + 2} - \sqrt{n + 1})$
- 35)  $\lim_{n \rightarrow \infty} (\sqrt{n + 3} - \sqrt{n - 5})$
- 36)  $\lim_{n \rightarrow \infty} (\sqrt{n^2 - n + 3} - n)$
- 37)  $\lim_{n \rightarrow \infty} \frac{1}{\sqrt{n+2} - \sqrt{n+1}}$

**GIỚI HẠN HÀM SỐ**

1.  $\lim_{x \rightarrow 2} (3x^2 + 7x + 11)$
2.  $\lim_{x \rightarrow 1} \frac{(7x + 11)x}{4x^2 + 2}$
3.  $\lim_{x \rightarrow -2} \frac{(3x + 1)(2 - 3x)}{x + 1}$
4.  $\lim_{x \rightarrow 0} 2x \left( 1 - \frac{7x + 11}{x} \right)$
5.  $\lim_{x \rightarrow \sqrt{3}} |x^2 - 4|$
6.  $\lim_{x \rightarrow 9} \frac{\sqrt{x} - 3}{9x - x^2}$
7.  $\lim_{x \rightarrow -\infty} \frac{3x^2 - x + 5}{x^3 - 2}$
8.  $\lim_{x \rightarrow -\infty} \frac{2x^4 - 3x + 5}{x^4 - 2x^2}$
9.  $\lim_{x \rightarrow +\infty} \frac{\sqrt{3x^6 - 2x^5 + 5}}{3x^3 - 2}$
10.  $\lim_{x \rightarrow -\infty} \frac{\sqrt{x^6 - 5x + 1}}{5x^3 - 2}$
11.  $\lim_{x \rightarrow -\infty} \sqrt[3]{\frac{x^2 + 5}{6x^2 - 3x + 2}}$
12.  $\lim_{x \rightarrow 3^+} \frac{|3-x|}{3-x}$
13.  $\lim_{x \rightarrow 3^-} \frac{|3-x|}{3-x}$
14.  $\lim_{x \rightarrow 3} \frac{|3-x|}{3-x}$
15.  $\lim_{x \rightarrow 0^+} \frac{x + 2\sqrt{x}}{x - \sqrt{x}}$
16.  $\lim_{x \rightarrow 2^-} \frac{4 - x^2}{\sqrt{2-x}}$
17.  $\lim_{x \rightarrow -\sqrt{2}} \frac{x^3 + 2\sqrt{2}}{x^2 - 2}$
18.  $\lim_{x \rightarrow 3} \frac{x^4 - 27x}{2x^2 - 3x - 9}$
19.  $\lim_{x \rightarrow -2} \frac{x^4 - 16}{x^2 + 6x + 8}$
20.  $\lim_{x \rightarrow +\infty} \sqrt[3]{\frac{2x^5 + x^3 - 1}{(2x^2 - 1)(x^3 + x)}}$
21.  $\lim_{x \rightarrow -\infty} \frac{\sqrt{x^2 + x + 2x}}{2x + 3}$
22.  $\lim_{x \rightarrow +\infty} (x + 1) \sqrt{\frac{x}{2x^4 + x^2 + 1}}$
23.  $\lim_{x \rightarrow +\infty} (2x^3 - 5x^2 + 3x - 1)$
24.  $\lim_{x \rightarrow +\infty} \sqrt{2x^4 - 5x^2 + 1}$

25.  $\lim_{x \rightarrow 2^+} \frac{2x+1}{x-2}$       26.  $\lim_{x \rightarrow 2^-} \frac{2x+1}{x-2}$       27.  $\lim_{x \rightarrow +\infty} (2x^3 - 5x^2 + 3x - 1)$       28.  $\lim_{x \rightarrow +\infty} \frac{x^3 - 5}{x^2 + 1}$   
 29.  $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x^2 - 4}$       31.  $\lim_{x \rightarrow (-3)^-} \frac{2x^2 + 5x - 3}{(x+3)^2}$       32.  $\lim_{x \rightarrow 0} \frac{\sqrt{x^3 + 1} - 1}{x^2 + x}$       33.  $\lim_{x \rightarrow +\infty} \frac{2x^2 + x + 10}{9 - 3x^3}$   
 34.  $\lim_{x \rightarrow -\sqrt{3}} \frac{x^3 + 3\sqrt{3}}{x^2 - 3}$       35.  $\lim_{x \rightarrow 4} \frac{\sqrt{x} - 2}{x^2 - 4x}$       36.  $\lim_{x \rightarrow 1^+} \frac{\sqrt{x-1}}{x^2 - x}$       37.  $\lim_{x \rightarrow 0} \frac{\sqrt{x^2 + x + 1} - 1}{3x}$   
 38.  $\lim_{x \rightarrow 3^-} \frac{3-x}{\sqrt{27-x^3}}$       39.  $\lim_{x \rightarrow 2^+} \frac{\sqrt{x^3 - 8}}{x^2 - 2x}$       40)  $\lim_{x \rightarrow 2} \frac{x^2 + 3x - 10}{3x^2 - 5x - 2}$       41)  $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2}$       42)  $\lim_{x \rightarrow 1} \frac{x^2 - 4x + 3}{(x-1)^2}$   
 43)  $\lim_{x \rightarrow 1} \frac{x-1}{1-\sqrt{x}}$       44)  $\lim_{x \rightarrow 3} \frac{x^2 + 2x - 15}{x - 3}$       45)  $\lim_{x \rightarrow -5} \frac{x^2 + 2x - 15}{x + 5}$       46)  $\lim_{x \rightarrow 1} \frac{x^3 - 1}{x(x+5)-6}$       47)  $\lim_{x \rightarrow -4} \frac{x^2 + 3x - 4}{x^2 + 4x}$   
 48)  $\lim_{x \rightarrow -4} \frac{x^2 - 5x + 6}{x^2 - 12x + 20}$       49)  $\lim_{x \rightarrow -2} \frac{x^3 + 3x^2 + 2x}{x^2 - x - 6}$       50)  $\lim_{x \rightarrow 1} \frac{x^4 - 1}{x^2 + 2x - 3}$       51)  $\lim_{x \rightarrow -2} \frac{x^3 + 4x^2 + 4x}{x^2 - x - 6}$   
 52)  $\lim_{x \rightarrow 2} \frac{\sqrt{x^2 + 5} - 3}{x - 2}$ .      53)  $\lim_{x \rightarrow 7} \frac{\sqrt[4]{x+9} - 2}{x - 7}$       54)  $\lim_{x \rightarrow 5} \frac{5-x}{\sqrt{5} - \sqrt{x}}$       55)  $\lim_{x \rightarrow 2} \frac{\sqrt{3x-5} - 1}{x - 2}$   
 56)  $\lim_{x \rightarrow 0} \frac{x}{\sqrt{1+x-1}}$       57)  $\lim_{x \rightarrow -1} \frac{x+1}{\sqrt{6x^2 + 3 + 3x}}$       58)  $\lim_{x \rightarrow 0} \frac{\sqrt{1+x+x^2} - 1}{x}$       59)  $\lim_{x \rightarrow 5} \frac{\sqrt{x+4} - 3}{x^2 - 25}$   
 60)  $\lim_{x \rightarrow 0} \frac{\sqrt{1-2x+x^2} - (1+x)}{x}$       61)  $\lim_{x \rightarrow 3} \frac{x-3}{\sqrt{2x+10}-4}$       62)  $\lim_{x \rightarrow 6} \frac{\sqrt{x-2}-2}{x-6}$       63)  $\lim_{x \rightarrow 1} \frac{2x-\sqrt{3x+1}}{x^2-1}$   
 64)  $\lim_{x \rightarrow 1} \frac{\sqrt{x}-1}{x^2+2x-3}$       65)  $\lim_{x \rightarrow 0} \frac{\sqrt{5+x} - \sqrt{5-x}}{x}$       66)  $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - \sqrt{1-x}}{x}$       67)  $\lim_{x \rightarrow 1} \frac{\sqrt{2x-1} - \sqrt{x}}{x-1}$   
 68)  $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - \sqrt{x^2+x+1}}{x}$       69)  $\lim_{x \rightarrow 1} \frac{\sqrt{3x-2} - \sqrt{4x^2-x-2}}{x^2-3x+2}$       70)  $\lim_{x \rightarrow 0} \frac{\sqrt{1-3x+x^2} - \sqrt{1+x}}{x}$   
 71)  $\lim_{x \rightarrow 4} \frac{3-\sqrt{5+x}}{1-\sqrt{5-x}}$       72)  $\lim_{x \rightarrow 2} \frac{x-\sqrt{x+2}}{\sqrt{4x+1}-3}$       73)  $\lim_{x \rightarrow 1} \frac{x^2-\sqrt{x}}{\sqrt{x}-1}$       74)  $\lim_{x \rightarrow -1} \frac{\sqrt[3]{x}+1}{\sqrt{x^2+3}-2}$       75)  $\lim_{x \rightarrow 0} \frac{\sqrt{4-x^2}-2}{\sqrt{9-x^2}-3}$   
 76)  $\lim_{x \rightarrow 9} \frac{\sqrt{7+2x}-5}{\sqrt{x}-3}$       77)  $\lim_{x \rightarrow +\infty} \frac{x^2+3x-10}{3x^2-5x-2}$       78)  $\lim_{x \rightarrow -\infty} \frac{x^2-4}{x^3-2}$       79)  $\lim_{x \rightarrow +\infty} \frac{x^2-4x+3}{(x-1)^2}$   
 80)  $\lim_{x \rightarrow -\infty} \frac{\sqrt{x^2+2x-15}}{x+5}$       81)  $\lim_{x \rightarrow +\infty} \sqrt{\frac{x^2-1}{x(x+5)-6}}$       82)  $\lim_{x \rightarrow -\infty} \frac{x^2+3x-4}{\sqrt{x^4+4x}}$       83)  $\lim_{x \rightarrow +\infty} \frac{\sqrt{x^4-5x^3+6}}{x^2-12x+20}$   
 84)  $\lim_{x \rightarrow -\infty} \frac{x^3+3x^2+2x}{x^5-x-6}$       85)  $\lim_{x \rightarrow -\infty} \frac{x-1}{x^2+2x-3}$       86)  $\lim_{x \rightarrow -\infty} \frac{\sqrt[3]{x^6-4x^4+4}}{x^2-x-6}$   
 87)  $\lim_{x \rightarrow -2^+} \frac{\sqrt{8+2x}-2}{\sqrt{x+2}}$       88)  $\lim_{x \rightarrow 0^+} \frac{2\sqrt{x}-3x}{3\sqrt{x}-2x}$       89)  $f(x) = \begin{cases} 3x-1 & ; x \leq 1 \\ x^2+1 & ; x > 1 \end{cases}$  tìm  $\lim_{x \rightarrow 1} f(x)$   
 90)  $f(x) = \begin{cases} mx^2 & ; x \leq 2 \\ 3 & ; x > 2 \end{cases}$  Tìm  $\lim_{x \rightarrow 2} f(x)$       91)  $f(x) = \begin{cases} |x^2-5x+6| & ; x > 2 \\ mx+4 & ; x \leq 2 \end{cases}$ . Tìm m để hàm số có giới hạn  
 khi  $x \rightarrow 2$   
 92)  $\lim_{x \rightarrow +\infty} x \left( \sqrt{x^2+1} - \sqrt{x^2-2} \right)$       93)  $\lim_{x \rightarrow +\infty} \left( \sqrt{x^2-7x+1} - \sqrt{x^2-3x+2} \right)$       94)  $\lim_{x \rightarrow +\infty} \left( \sqrt{x^2-4x+1} - \sqrt{x^2-9x} \right)$   
 95)  $\lim_{x \rightarrow +\infty} \left( \sqrt{x^2-2x+1} - \sqrt{x^2-6x+3} \right)$       96)  $\lim_{x \rightarrow +\infty} \left( x-4 - \sqrt{x^2-7x+2} \right)$

# 60 BÀI TẬP GIỚI HẠN DÃY SỐ

1, $\lim \frac{n^2 - 2n + 1}{3n^2 + n - 3}$	2, $\lim \frac{(n+1)(n+2)}{-n^2 + 3n - 1}$	3, $\lim \frac{(n+1)(2n-5)}{(3n-1)(n+2)}$
4, $\lim \frac{n\sqrt{n} - n + 1}{n^2 + 3}$	5, $\lim \frac{n^3 - 4n + 1}{-4n^3 + n^2 - 2}$	6, $\lim \frac{n+3}{n + (-1)^n}$
7, $\lim \sqrt{\frac{4n+6}{n-1}}$	8, $\lim \frac{(n+1)^2 - 3n}{(2n-1)^2}$	9, $\lim \frac{(n+1)^4 - (n-1)^4}{(n+1)^4 + (n-1)^4}$
10, $\lim \frac{(n^2-1)(3n+2)}{-n^3 + 2n - 1}$	11, $\lim \frac{(n^2 + 3n + 6)(2n^2 - n - 1)}{8n^4 + 4n^3 - 1}$	12, $\lim \frac{(n^2 - 3)(-2n^2 + 4n - 1)}{(6n^3 + 2n - 1)(2n - 1)}$
13, $\lim \frac{\sqrt{4n^2 + n + 1}}{-n - 3}$	14, $\lim \frac{\sqrt{n^2 + 1} - 3n - 1}{-6n - \sqrt{n} + 1}$	15, $\lim \frac{\sqrt{n^3 + n^2 - 2n} - 4n}{-2n\sqrt{n} - 4n + 1}$
16, $\lim \frac{(2n-1)^{2007} - 1}{n^{2007} - 3n^{2000}}$	17, $\lim \frac{(3n-1)(n^2 + 2)(-3n^3 - 1)}{(2n^2 + 1)^3}$	18, $\lim \frac{\sqrt{n+1} - 2}{\sqrt{n} + 3}$
19, $\lim \frac{\sqrt[3]{8n^3 + 2n - 1} + 3n}{2n - 4\sqrt{n} + 7}$	20, $\lim \frac{\sqrt{2n^2 + 1} - \sqrt{n^2 + 1}}{n + 1}$	21, $\lim \frac{1+2+3+\dots+n}{n^2}$
22, $\lim \frac{n\sqrt{1+3+5+\dots+(2n+1)}}{3n^2 - n + 1}$	23, $\lim \frac{\sqrt{n^3 + 1} - \sqrt{n^2 + 2n}}{3n\sqrt{n} - 2n + 1}$	24, $\lim \frac{n(\sqrt{3n^2 + 1} + \sqrt{n^2 + 2n - 1})}{5n^2 - 3n + 2}$
25, $\lim \frac{\sqrt[3]{n^3 + 3n + 1} - \sqrt{3n^2 + 4}}{3n - 1}$	26, $\lim \frac{(5n^2 + 3n - 1)(2n^2 + 6)}{(2n+1)^4 - (3n-1)^4}$	27, $\lim \frac{\sqrt{n + 2\sqrt{n}}(3n - 1)}{n\sqrt{n} - 2n + 6}$
28, $\lim \frac{\sqrt{4n+1}(2n^2 - 4n + 2)}{\sqrt{n^5 + 3n - 1}}$	29, $\lim \frac{\sqrt{n^2 - n + 3}(4n - 7)}{2n^2 + 4}$	30, $\lim \frac{\sqrt[3]{n^3 + 7}(\sqrt{4n^2 - 1} + 2n - 1)}{(3n - 2)^2}$
31, $\lim \frac{2^n + 3^n}{3^n + 1}$	32, $\lim \frac{2^{n+1} + 3^{n+1}}{2^n + 3^n}$	33, $\lim \frac{(-2)^n + 3^n}{(-2)^n - 3^{n+1}}$
34, $\lim \frac{5^n - 3^n}{5^{n+1} + 3^{n+2}}$	35, $\lim (n^2 - 3n - 10)$	36, $\lim (-n^3 + 4n - 1)$
37, $\lim (-2n^4 - 3\sqrt{n} + 1)$	38, $\lim (2n - \sqrt{n^3} + 1)$	39, $\lim (\sqrt{n} - \sqrt[3]{n} + 1)$
40, $\lim \frac{2n^2 - n}{n + 1}$	41, $\lim \frac{3n^2 + 3n - 1}{2n^3 - 2n + 1}$	42, $\lim \frac{(n-1)^2 - \sqrt{n}}{3n + 2}$
43, $\lim \frac{(2n-1)^3 + n^3 - 2n + 1}{2n^4 + 3n - 2}$	44, $\lim \frac{(2n^2 - 1)^2 - (n+1)^4}{(4n+3)^3}$	45, $\lim \frac{n\sqrt{n} + 3n - 1}{5n + 7}$
46, $\lim (\sqrt{n^2 + n + 5} - n)$	47, $\lim (\sqrt{4n^2 - 3n + 1} - 2n)$	48, $\lim (\sqrt{n^2 + 2} - n)n$
49, $\lim (\sqrt{n^2 + 2} - n)$	50, $\lim (\sqrt{n^2 - 3n + 1} - 2n)$	51, $\lim (\sqrt{n^2 + 4n + 2} - n + 2)$
52, $\lim (\sqrt{2n^2 + 1} - \sqrt{2n^2 + n + 1})$	53, $\lim \sqrt{n}(\sqrt{n+3} - \sqrt{n+1})$	54, $\lim \sqrt{n+5}(\sqrt{2n+3} - \sqrt{2n-1})$
55, $\lim \frac{1}{n+1 - \sqrt{n^2 + 2}}$	56, $\lim \frac{\sqrt{2n+1} - \sqrt{n}}{\sqrt{2n-5} - \sqrt{n+2}}$	57, $\lim \frac{\sqrt{3n+2}(\sqrt{2n-1} - \sqrt{n-2})}{\sqrt{n} + 3}$
58, $\lim (\sqrt[3]{n^3 + 2n^2 + 1} - n)$	59, $\lim (\sqrt{n^2 + 3n} + \sqrt[3]{n^3 + n^2} - 2n)$	60, $\lim (\sqrt[3]{n^3 + 3n^2 + 1} - \sqrt{n^2 + 2n})$